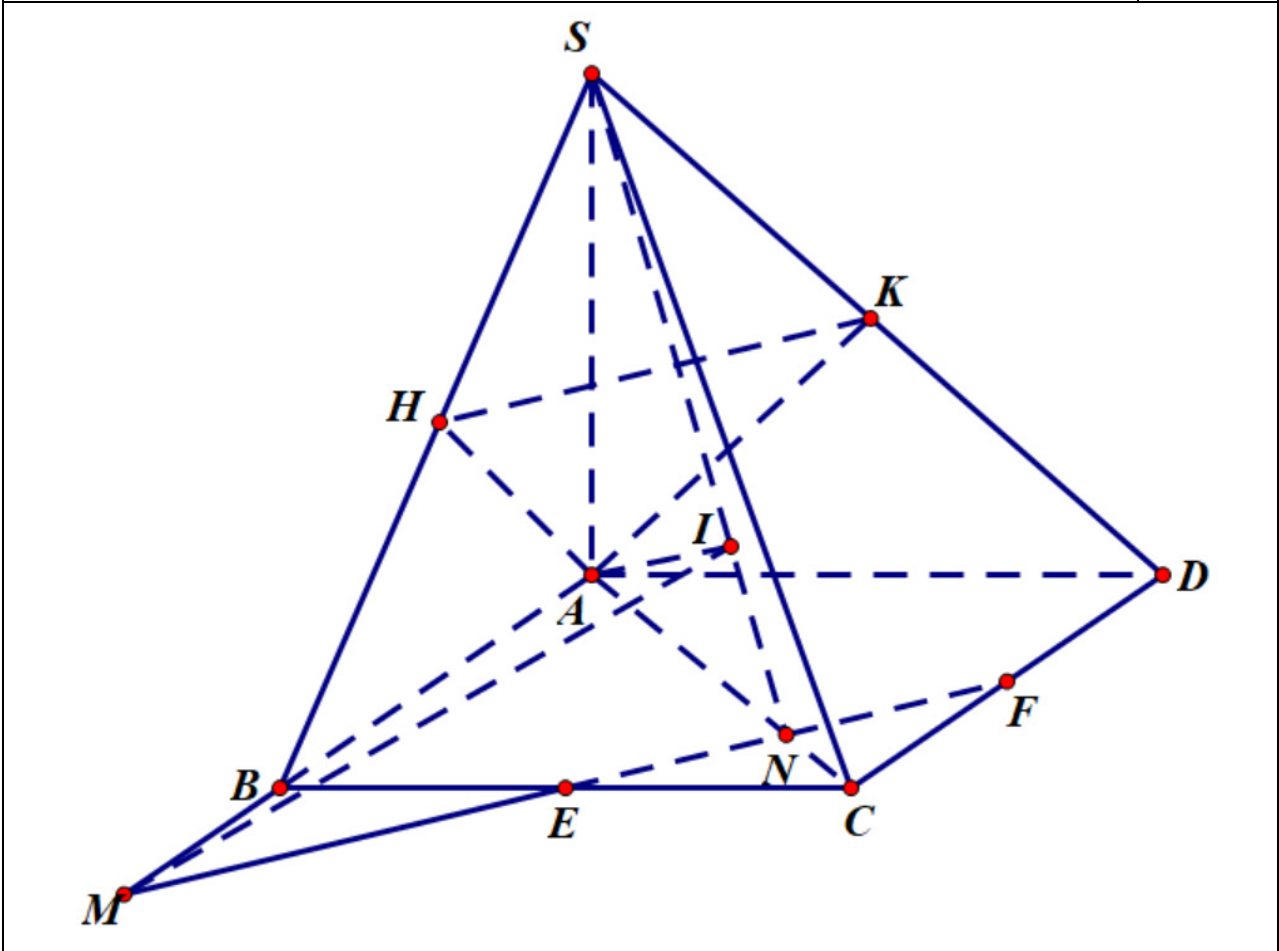


ĐÁP ÁN & BIỂU ĐIỂM TOÁN 11 – KTGHK2 (2018–2019)

Bài 1a:	1.5đ
$\lim_{x \rightarrow -1} \frac{(2x+1)^2 - x^2}{x^3 + 3x^2 - 4x - 6} = \lim_{x \rightarrow -1} \frac{(x+1)(3x+1)}{(x+1)(x^2 + 2x - 6)} = \lim_{x \rightarrow -1} \frac{3x+1}{x^2 + 2x - 6} = \frac{2}{7}$	0.5 x 3
Bài 1b:	1.5đ
$\lim_{x \rightarrow 3} \frac{2\sqrt{4x-3} - 3\sqrt{x+1}}{x-3} = \lim_{x \rightarrow 3} \frac{7(x-3)}{(x-3)(2\sqrt{4x-3} + 3\sqrt{x+1})} = \lim_{x \rightarrow 3} \frac{7}{2\sqrt{4x-3} + 3\sqrt{x+1}} = \frac{7}{12}$	0.5 x 3
Bài 1c:	2đ
$\lim_{x \rightarrow +\infty} (\sqrt{4x^2 + x} + \sqrt[3]{1-8x^3}) = \lim_{x \rightarrow +\infty} (\sqrt{4x^2 + x} - 2x + 2x - \sqrt[3]{8x^3 - 1})$ $= \lim_{x \rightarrow +\infty} \left(\frac{x}{\sqrt{4x^2 + x} + 2x} + \frac{1}{(\sqrt[3]{8x^3 - 1})^2 + 2x\sqrt[3]{8x^3 - 1} + 4x^2} \right)$ $= \lim_{x \rightarrow +\infty} \left(\frac{1}{\sqrt{4 + \frac{1}{x}} + 2} + \frac{1}{x^2} \cdot \frac{1}{\left(\sqrt[3]{8 - \frac{1}{x^3}}\right)^2 + 2\sqrt[3]{8 - \frac{1}{x^3}} + 4} \right) = \frac{1}{4}$	0.5 0.5 x 2 0.25 x 2
Bài 2a:	1.5đ
$\begin{cases} BC \perp AB \\ BC \perp SA \end{cases} \Rightarrow BC \perp (SAB)$	0.5 x 3
Bài 2b:	1.5đ
$\begin{cases} BD \perp AC \\ BD \perp SA \end{cases} \Rightarrow BD \perp (SAC)$	0.5 x 2
• $EF \parallel BD$. Suy ra $EF \perp (SAC) \Rightarrow EF \perp SC$	0.5
Bài 2c:	1đ
H là trung điểm SB. Gọi K là trung điểm SD, suy ra $HK \parallel BD \parallel EF$ $\Rightarrow (\widehat{AH, EF}) = (\widehat{AH, HK})$	0.25 0.25
ΔSAB vuông cân: $AH = \frac{SB}{2} = \frac{a\sqrt{2}}{2} = AK$; $HK = \frac{BD}{2} = \frac{a\sqrt{2}}{2}$ Nên ΔAHK đều. Suy ra $(\widehat{AH, HK}) = \widehat{AHK} = 60^\circ$	0.25 0.25
Bài 2d:	1đ
Gọi $N = EF \cap AC$. Kẻ $AI \perp SN$. Suy ra $AI \perp (SEF)$. Gọi $M = EF \cap AB \Rightarrow MI$ là hình chiếu của AB lên (SEF)	0.25

hay $\left(\widehat{AB, (SEF)}\right) = \left(\widehat{AB, MI}\right) = \widehat{AMI}$	0.25
• $AN = \frac{3}{4}AC = \frac{3a\sqrt{2}}{4} \Rightarrow AI = \frac{3a}{\sqrt{17}}$	0.25
• $AM = \frac{3}{2}AB = \frac{3a}{2} \Rightarrow \sin \widehat{AMI} = \frac{AI}{AM} = \frac{2}{\sqrt{17}} \Rightarrow \widehat{AMI} = \arcsin \frac{2}{\sqrt{17}}$	0.25



HẾT